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Contextural operations on sub-signs

1. As Kronthaler (1986, pp. 36 ss.) and Toth (2003, pp. 36 ss.) have shown extensively, there are two kinds of operators on qualitative numbers: intra- and inter- (or trans-) operators. Intra-operators work inside of a contexture, inter-operators between contextures. As it is known from elementary semiotic arithmetic, sub-signs can be changed by adding the unit of a representation value (Rpv) to either the triadic or the trichotomic value. Thus, by simple addition or subtraction of $Rpv = 1$, one can produce the complete semiotic matrix, f. ex.

$$(1.1) + (0.1) = (1.2); (1.1) + (1.0) = (2.1); (1.1) + (1.1) + (1.0) = (3.2), \text{ etc.}$$

$$\left(\begin{array}{ccc} 1.1_{1,3} & 1.2_1 & 1.3_3 \\ 2.1_1 & 2.2_{1,2} & 2.3_2 \\ 3.1_3 & 3.2_2 & 3.3_{2,3} \end{array} \right)$$

2. Changing sub-signs by addition of $Cv = +1$

$$\begin{array}{ccc} 1.1_{1,3} & 1.2_1 & 1.3_3 \\ +1,0 & +1,0 & +1,0 \\ \hline 1.1_{2,3} & 1.2_2 & 1.3_4 \end{array}$$

(1.1) is now in the contextures of (3.3), (1.2) in the contexture of (2.3/3.4). The contexture of (1.3) is not defined over 3-cont. SR.

2.1 ₁	2.2 _{1,2}	2.3 ₂
+1,0	+1,0	+1,0
2.1 ₂	2.2 _{2,2}	2.3 ₄

(2.1) belongs now to the contexture of (2.3/3.2). (2.2) is excluded, since contextuated sub-signs cannot be self-referential! The new contexture of (2.3) is not defined over 3-cont. SR.

3.1 ₃	3.2 ₂	3.3 _{2,3}
+1,0	+1,0	+1,0
3.1 ₄	3.2 ₃	3.3 _{3,3}

The new contexture of (3.1) is not defined over 3-cont. SR. (3.2) is now in the contexture von (1.3/3.1). (3.3) would be again a case, where a sub-sign – in contrast with the abolishment of the logical law of identity – could be self-identical.

2. Changing sub-signs by subtraction of Cv = +1

1.1 _{1,3}	1.2 ₁	1.3 ₃
-1,0	-1,0	-1,0
1.1 _{0,3}	1.2 ₀	1.3 ₂

(1.1) is now in the contextures of (1.3/3.1), (1.2) in the contexture 0, which is not defined. (1.3) is now in the constructure (1.2/2.1).

2.1 ₁	2.2 _{1,2}	2.3 ₂
-1,0	-1,0	-1,0

2.1 ₀	2.2 _{0,2}	2.3 ₁

A contexture 0 is not defined. (2.2)₂ is excluded, since identitive morphisms must have at least two (different) indices. (2.3) is not in the contexture of (1.2/2.1).

3.1 ₃	3.2 ₂	3.3 _{2,3}
-1,0	-1,0	-1,0

3.1 ₂	3.2 ₁	3.3 _{1,3}

(3.1) is now in the contexture of (2.3/(3.2)), (3.2) in the contexture of (1.2/2.1), and (3.3) is in the contexture of (1.1).

As one sees, by simple addition or subtraction, one can reach any other of the several n-contextural matrices (cf. Toth 2009).

Bibliography

- Kronthaler, Engelbert, Grundlegung einer Mathematik der Qualitäten. Frankfurt am Mein 1986
 Toth, Alfred Die Hiochzeit von Semiotik und Struktur. Klagenfurt 2003
 Toth, Alfred, Polycontextural matrices. In: Electronic Journal for Mathematical Semiotics, <http://www.mathematical-semiotics.com/pdf/Polycont.%20matr..pdf> (2009)

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